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Table 1 Binomial Distribution Cumulative Probabilities

Let X be a binomial random variable with parameters n and p : $X \sim B(n, p)$. This table contains cumulative probabilities:

$$P(X \leq x) = \sum_{k=0}^x P(X = k) = P(X = 0) + P(X = 1) + P(X = 2) + \dots + P(X = x).$$

$n = 5$		p													
x	0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
0	0.9510	0.7738	0.5905	0.3277	0.2373	0.1681	0.0778	0.0313	0.0102	0.0024	0.0010	0.0003	0.0000		
1	0.9990	0.9774	0.9185	0.7373	0.6328	0.5282	0.3370	0.1875	0.0870	0.0308	0.0156	0.0067	0.0005	0.0000	
2	1.0000	0.9988	0.9914	0.9421	0.8965	0.8369	0.6826	0.5000	0.3174	0.1631	0.1035	0.0579	0.0086	0.0012	0.0000
3		1.0000	0.9995	0.9933	0.9844	0.9692	0.9130	0.8125	0.6630	0.4718	0.3672	0.2627	0.0815	0.0226	0.0010
4			1.0000	0.9997	0.9990	0.9976	0.9898	0.9688	0.9222	0.8319	0.7627	0.6723	0.4095	0.2262	0.0490

$n = 10$		p													
x	0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
0	0.9044	0.5987	0.3487	0.1074	0.0563	0.0282	0.0060	0.0010	0.0001	0.0000					
1	0.9957	0.9139	0.7361	0.3758	0.2440	0.1493	0.0464	0.0107	0.0017	0.0001	0.0000	0.0000			
2	0.9999	0.9885	0.9298	0.6778	0.5256	0.3828	0.1673	0.0547	0.0123	0.0016	0.0004	0.0001	0.0000		
3	1.0000	0.9990	0.9872	0.8791	0.7759	0.6496	0.3823	0.1719	0.0548	0.0106	0.0035	0.0009	0.0000		
4		0.9999	0.9984	0.9672	0.9219	0.8497	0.6331	0.3770	0.1662	0.0473	0.0197	0.0064	0.0001	0.0000	
5		1.0000	0.9999	0.9936	0.9803	0.9527	0.8338	0.6230	0.3669	0.1503	0.0781	0.0328	0.0016	0.0001	
6			1.0000	0.9991	0.9965	0.9894	0.9452	0.8281	0.6177	0.3504	0.2241	0.1209	0.0128	0.0010	0.0000
7				0.9999	0.9996	0.9984	0.9877	0.9453	0.8327	0.6172	0.4744	0.3222	0.0702	0.0115	0.0001
8				1.0000	1.0000	0.9999	0.9983	0.9893	0.9536	0.8507	0.7560	0.6242	0.2639	0.0861	0.0043
9						1.0000	0.9999	0.9990	0.9940	0.9718	0.9437	0.8926	0.6513	0.4013	0.0956

$n = 15$		p													
x	0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
0	0.8601	0.4633	0.2059	0.0352	0.0134	0.0047	0.0005	0.0000							
1	0.9904	0.8290	0.5490	0.1671	0.0802	0.0353	0.0052	0.0005	0.0000						
2	0.9996	0.9638	0.8159	0.3980	0.2361	0.1268	0.0271	0.0037	0.0003	0.0000					
3	1.0000	0.9945	0.9444	0.6482	0.4613	0.2969	0.0905	0.0176	0.0019	0.0001	0.0000				
4		0.9994	0.9873	0.8358	0.6865	0.5155	0.2173	0.0592	0.0093	0.0007	0.0001	0.0000			
5		0.9999	0.9978	0.9389	0.8516	0.7216	0.4032	0.1509	0.0338	0.0037	0.0008	0.0001			
6		1.0000	0.9997	0.9819	0.9434	0.8689	0.6098	0.3036	0.0950	0.0152	0.0042	0.0008			
7			1.0000	0.9958	0.9827	0.9500	0.7869	0.5000	0.2131	0.0500	0.0173	0.0042	0.0000		
8				0.9992	0.9958	0.9848	0.9050	0.6964	0.3902	0.1311	0.0566	0.0181	0.0003	0.0000	
9				0.9999	0.9992	0.9963	0.9662	0.8491	0.5968	0.2784	0.1484	0.0611	0.0022	0.0001	
10				1.0000	0.9999	0.9993	0.9907	0.9408	0.7827	0.4845	0.3135	0.1642	0.0127	0.0006	
11					1.0000	0.9999	0.9981	0.9824	0.9095	0.7031	0.5387	0.3518	0.0556	0.0055	0.0000
12						1.0000	0.9997	0.9963	0.9729	0.8732	0.7639	0.6020	0.1841	0.0362	0.0004
13							1.0000	0.9995	0.9948	0.9647	0.9198	0.8329	0.4510	0.1710	0.0096
14								1.0000	0.9995	0.9953	0.9866	0.9648	0.7941	0.5367	0.1399

Table 1 Binomial Distribution Cumulative Probabilities (Continued)

<i>n</i> = 20		<i>p</i>													
<i>x</i>	0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
0	0.8179	0.3585	0.1216	0.0115	0.0032	0.0008	0.0000								
1	0.9831	0.7358	0.3917	0.0692	0.0243	0.0076	0.0005	0.0000							
2	0.9990	0.9245	0.6769	0.2061	0.0913	0.0355	0.0036	0.0002							
3	1.0000	0.9841	0.8670	0.4114	0.2252	0.1071	0.0160	0.0013	0.0000						
4		0.9974	0.9568	0.6296	0.4148	0.2375	0.0510	0.0059	0.0003						
5		0.9997	0.9887	0.8042	0.6172	0.4164	0.1256	0.0207	0.0016	0.0000					
6		1.0000	0.9976	0.9133	0.7858	0.6080	0.2500	0.0577	0.0065	0.0003	0.0000				
7			0.9996	0.9679	0.8982	0.7723	0.4159	0.1316	0.0210	0.0013	0.0002	0.0000			
8			0.9999	0.9900	0.9591	0.8867	0.5956	0.2517	0.0565	0.0051	0.0009	0.0001			
9			1.0000	0.9974	0.9861	0.9520	0.7553	0.4119	0.1275	0.0171	0.0039	0.0006			
10				0.9994	0.9961	0.9829	0.8725	0.5881	0.2447	0.0480	0.0139	0.0026	0.0000		
11				0.9999	0.9991	0.9949	0.9435	0.7483	0.4044	0.1133	0.0409	0.0100	0.0001		
12				1.0000	0.9998	0.9987	0.9790	0.8684	0.5841	0.2277	0.1018	0.0321	0.0004		
13					1.0000	0.9997	0.9935	0.9423	0.7500	0.3920	0.2142	0.0867	0.0024	0.0000	
14						1.0000	0.9984	0.9793	0.8744	0.5836	0.3828	0.1958	0.0113	0.0003	
15							0.9997	0.9941	0.9490	0.7625	0.5852	0.3704	0.0432	0.0026	
16							1.0000	0.9987	0.9840	0.8929	0.7748	0.5886	0.1330	0.0159	0.0000
17								0.9998	0.9964	0.9645	0.9087	0.7939	0.3231	0.0755	0.0010
18								1.0000	0.9995	0.9924	0.9757	0.9308	0.6083	0.2642	0.0169
19									1.0000	0.9992	0.9968	0.9885	0.8784	0.6415	0.1821

<i>n</i> = 25		<i>p</i>													
<i>x</i>	0.01	0.05	0.10	0.20	0.25	0.30	0.40	0.50	0.60	0.70	0.75	0.80	0.90	0.95	0.99
0	0.7778	0.2774	0.0718	0.0038	0.0008	0.0001	0.0000								
1	0.9742	0.6424	0.2712	0.0274	0.0070	0.0016	0.0001								
2	0.9980	0.8729	0.5371	0.0982	0.0321	0.0090	0.0004	0.0000							
3	0.9999	0.9659	0.7636	0.2340	0.0962	0.0332	0.0024	0.0001							
4	1.0000	0.9928	0.9020	0.4207	0.2137	0.0905	0.0095	0.0005	0.0000						
5		0.9988	0.9666	0.6167	0.3783	0.1935	0.0294	0.0020	0.0001						
6		0.9998	0.9905	0.7800	0.5611	0.3407	0.0736	0.0073	0.0003						
7		1.0000	0.9977	0.8909	0.7265	0.5118	0.1536	0.0216	0.0012	0.0000					
8			0.9995	0.9532	0.8506	0.6769	0.2735	0.0539	0.0043	0.0001					
9			0.9999	0.9827	0.9287	0.8106	0.4246	0.1148	0.0132	0.0005	0.0000				
10			1.0000	0.9944	0.9703	0.9022	0.5858	0.2122	0.0344	0.0018	0.0002	0.0000			
11				0.9985	0.9893	0.9558	0.7323	0.3450	0.0778	0.0060	0.0009	0.0001			
12				0.9996	0.9966	0.9825	0.8462	0.5000	0.1538	0.0175	0.0034	0.0004			
13				0.9999	0.9991	0.9940	0.9222	0.6550	0.2677	0.0442	0.0107	0.0015			
14				1.0000	0.9998	0.9982	0.9656	0.7878	0.4142	0.0978	0.0297	0.0056	0.0000		
15					1.0000	0.9995	0.9868	0.8852	0.5754	0.1894	0.0713	0.0173	0.0001		
16						0.9999	0.9957	0.9461	0.7265	0.3231	0.1494	0.0468	0.0005		
17						1.0000	0.9988	0.9784	0.8464	0.4882	0.2735	0.1091	0.0023	0.0000	
18							0.9997	0.9927	0.9264	0.6593	0.4389	0.2200	0.0095	0.0002	
19							0.9999	0.9980	0.9706	0.8065	0.6217	0.3833	0.0334	0.0012	
20							1.0000	0.9995	0.9905	0.9095	0.7863	0.5793	0.0980	0.0072	0.0000
21								0.9999	0.9976	0.9668	0.9038	0.7660	0.2364	0.0341	0.0001
22								1.0000	0.9996	0.9910	0.9679	0.9018	0.4629	0.1271	0.0020
23									0.9999	0.9984	0.9930	0.9726	0.7288	0.3576	0.0258
24									1.0000	0.9999	0.9992	0.9962	0.9282	0.7226	0.2222

Table 2 Poisson Distribution Cumulative Probabilities

Let X be a Poisson random variable with parameter λ . This table contains cumulative probabilities:

$$P(X \leq x) = \sum_{k=0}^x P(X = k) = P(X = 0) + P(X = 1) + \dots + P(X = x).$$

x	λ									
	0.05	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50
0	0.9512	0.9048	0.8607	0.8187	0.7788	0.7408	0.7047	0.6703	0.6376	0.6065
1	0.9988	0.9953	0.9898	0.9825	0.9735	0.9631	0.9513	0.9384	0.9246	0.9098
2	1.0000	0.9998	0.9995	0.9989	0.9978	0.9964	0.9945	0.9921	0.9891	0.9856
3		1.0000	1.0000	0.9999	0.9999	0.9997	0.9995	0.9992	0.9988	0.9982
4				1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998
5								1.0000	1.0000	1.0000

x	λ									
	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
0	0.5769	0.5488	0.5220	0.4966	0.4724	0.4493	0.4274	0.4066	0.3867	0.3679
1	0.8943	0.8781	0.8614	0.8442	0.8266	0.8088	0.7907	0.7725	0.7541	0.7358
2	0.9815	0.9769	0.9717	0.9659	0.9595	0.9526	0.9451	0.9371	0.9287	0.9197
3	0.9975	0.9966	0.9956	0.9942	0.9927	0.9909	0.9889	0.9865	0.9839	0.9810
4	0.9997	0.9996	0.9994	0.9992	0.9989	0.9986	0.9982	0.9977	0.9971	0.9963
5	1.0000	1.0000	0.9999	0.9999	0.9999	0.9998	0.9997	0.9997	0.9995	0.9994
6		1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999
7									1.0000	1.0000

x	λ									
	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9	2.0
0	0.3329	0.3012	0.2725	0.2466	0.2231	0.2019	0.1827	0.1653	0.1496	0.1353
1	0.6990	0.6626	0.6268	0.5918	0.5578	0.5249	0.4932	0.4628	0.4337	0.4060
2	0.9004	0.8795	0.8571	0.8335	0.8088	0.7834	0.7572	0.7306	0.7037	0.6767
3	0.9743	0.9662	0.9569	0.9463	0.9344	0.9212	0.9068	0.8913	0.8747	0.8571
4	0.9946	0.9923	0.9893	0.9857	0.9814	0.9763	0.9704	0.9636	0.9559	0.9473
5	0.9990	0.9985	0.9978	0.9968	0.9955	0.9940	0.9920	0.9896	0.9868	0.9834
6	0.9999	0.9997	0.9996	0.9994	0.9991	0.9987	0.9981	0.9974	0.9966	0.9955
7	1.0000	1.0000	0.9999	0.9999	0.9998	0.9997	0.9996	0.9994	0.9992	0.9989
8			1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9998
9						1.0000	1.0000	1.0000	1.0000	1.0000

Table 2 Poisson Distribution Cumulative Probabilities (Continued)

x	λ									
	2.1	2.2	2.3	2.4	2.5	2.6	2.7	2.8	2.9	3.0
0	0.1225	0.1108	0.1003	0.0907	0.0821	0.0743	0.0672	0.0608	0.0550	0.0498
1	0.3796	0.3546	0.3309	0.3084	0.2873	0.2674	0.2487	0.2311	0.2146	0.1991
2	0.6496	0.6227	0.5960	0.5697	0.5438	0.5184	0.4936	0.4695	0.4460	0.4232
3	0.8386	0.8194	0.7993	0.7787	0.7576	0.7360	0.7141	0.6919	0.6696	0.6472
4	0.9379	0.9275	0.9162	0.9041	0.8912	0.8774	0.8629	0.8477	0.8318	0.8153
5	0.9796	0.9751	0.9700	0.9643	0.9580	0.9510	0.9433	0.9349	0.9258	0.9161
6	0.9941	0.9925	0.9906	0.9884	0.9858	0.9828	0.9794	0.9756	0.9713	0.9665
7	0.9985	0.9980	0.9974	0.9967	0.9958	0.9947	0.9934	0.9919	0.9901	0.9881
8	0.9997	0.9995	0.9994	0.9991	0.9989	0.9985	0.9981	0.9976	0.9969	0.9962
9	0.9999	0.9999	0.9999	0.9998	0.9997	0.9996	0.9995	0.9993	0.9991	0.9989
10	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9998	0.9998	0.9997
11				1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999
12									1.0000	1.0000

x	λ									
	3.1	3.2	3.3	3.4	3.5	3.6	3.7	3.8	3.9	4.0
0	0.0450	0.0408	0.0369	0.0334	0.0302	0.0273	0.0247	0.0224	0.0202	0.0183
1	0.1847	0.1712	0.1586	0.1468	0.1359	0.1257	0.1162	0.1074	0.0992	0.0916
2	0.4012	0.3799	0.3594	0.3397	0.3208	0.3027	0.2854	0.2689	0.2531	0.2381
3	0.6248	0.6025	0.5803	0.5584	0.5366	0.5152	0.4942	0.4735	0.4532	0.4335
4	0.7982	0.7806	0.7626	0.7442	0.7254	0.7064	0.6872	0.6678	0.6484	0.6288
5	0.9057	0.8946	0.8829	0.8705	0.8576	0.8441	0.8301	0.8156	0.8006	0.7851
6	0.9612	0.9554	0.9490	0.9421	0.9347	0.9267	0.9182	0.9091	0.8995	0.8893
7	0.9858	0.9832	0.9802	0.9769	0.9733	0.9692	0.9648	0.9599	0.9546	0.9489
8	0.9953	0.9943	0.9931	0.9917	0.9901	0.9883	0.9863	0.9840	0.9815	0.9786
9	0.9986	0.9982	0.9978	0.9973	0.9967	0.9960	0.9952	0.9942	0.9931	0.9919
10	0.9996	0.9995	0.9994	0.9992	0.9990	0.9987	0.9984	0.9981	0.9977	0.9972
11	0.9999	0.9999	0.9998	0.9998	0.9997	0.9996	0.9995	0.9994	0.9993	0.9991
12	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9999	0.9998	0.9998	0.9997
13				1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999
14									1.0000	1.0000

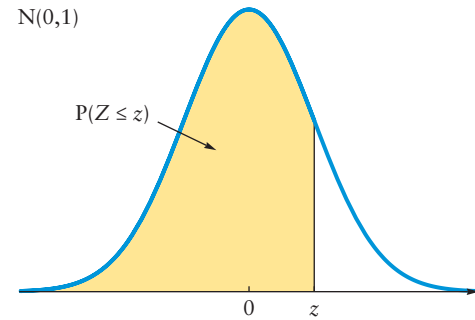
Table 2 Poisson Distribution Cumulative Probabilities (Continued)

x	λ									
	4.1	4.2	4.3	4.4	4.5	4.6	4.7	4.8	4.9	5.0
0	0.0166	0.0150	0.0136	0.0123	0.0111	0.0101	0.0091	0.0082	0.0074	0.0067
1	0.0845	0.0780	0.0719	0.0663	0.0611	0.0563	0.0518	0.0477	0.0439	0.0404
2	0.2238	0.2102	0.1974	0.1851	0.1736	0.1626	0.1523	0.1425	0.1333	0.1247
3	0.4142	0.3954	0.3772	0.3594	0.3423	0.3257	0.3097	0.2942	0.2793	0.2650
4	0.6093	0.5898	0.5704	0.5512	0.5321	0.5132	0.4946	0.4763	0.4582	0.4405
5	0.7693	0.7531	0.7367	0.7199	0.7029	0.6858	0.6684	0.6510	0.6335	0.6160
6	0.8786	0.8675	0.8558	0.8436	0.8311	0.8180	0.8046	0.7908	0.7767	0.7622
7	0.9427	0.9361	0.9290	0.9214	0.9134	0.9049	0.8960	0.8867	0.8769	0.8666
8	0.9755	0.9721	0.9683	0.9642	0.9597	0.9549	0.9497	0.9442	0.9382	0.9319
9	0.9905	0.9889	0.9871	0.9851	0.9829	0.9805	0.9778	0.9749	0.9717	0.9682
10	0.9966	0.9959	0.9952	0.9943	0.9933	0.9922	0.9910	0.9896	0.9880	0.9863
11	0.9989	0.9986	0.9983	0.9980	0.9976	0.9971	0.9966	0.9960	0.9953	0.9945
12	0.9997	0.9996	0.9995	0.9993	0.9992	0.9990	0.9988	0.9986	0.9983	0.9980
14	0.9999	0.9999	0.9998	0.9998	0.9997	0.9997	0.9996	0.9995	0.9994	0.9993
15	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9999	0.9999	0.9998	0.9998
16				1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999
17									1.0000	1.0000

x	λ									
	5.5	6.0	6.5	7.0	7.5	8.0	8.5	9.0	9.5	10.0
0	0.0041	0.0025	0.0015	0.0009	0.0006	0.0003	0.0002	0.0001	0.0001	0.0000
1	0.0266	0.0174	0.0113	0.0073	0.0047	0.0030	0.0019	0.0012	0.0008	0.0005
2	0.0884	0.0620	0.0430	0.0296	0.0203	0.0138	0.0093	0.0062	0.0042	0.0028
3	0.2017	0.1512	0.1118	0.0818	0.0591	0.0424	0.0301	0.0212	0.0149	0.0103
4	0.3575	0.2851	0.2237	0.1730	0.1321	0.0996	0.0744	0.0550	0.0403	0.0293
5	0.5289	0.4457	0.3690	0.3007	0.2414	0.1912	0.1496	0.1157	0.0885	0.0671
6	0.6860	0.6063	0.5265	0.4497	0.3782	0.3134	0.2562	0.2068	0.1649	0.1301
7	0.8095	0.7440	0.6728	0.5987	0.5246	0.4530	0.3856	0.3239	0.2687	0.2202
8	0.8944	0.8472	0.7916	0.7291	0.6620	0.5925	0.5231	0.4557	0.3918	0.3328
9	0.9462	0.9161	0.8774	0.8305	0.7764	0.7166	0.6530	0.5874	0.5218	0.4579
10	0.9747	0.9574	0.9332	0.9015	0.8622	0.8159	0.7634	0.7060	0.6453	0.5830
11	0.9890	0.9799	0.9661	0.9467	0.9208	0.8881	0.8487	0.8030	0.7520	0.6968
12	0.9955	0.9912	0.9840	0.9730	0.9573	0.9362	0.9091	0.8758	0.8364	0.7916
13	0.9983	0.9964	0.9929	0.9872	0.9784	0.9658	0.9486	0.9261	0.8981	0.8645
14	0.9994	0.9986	0.9970	0.9943	0.9897	0.9827	0.9726	0.9585	0.9400	0.9165
15	0.9998	0.9995	0.9988	0.9976	0.9954	0.9918	0.9862	0.9780	0.9665	0.9513
16	0.9999	0.9998	0.9996	0.9990	0.9980	0.9963	0.9934	0.9889	0.9823	0.9730
17	1.0000	0.9999	0.9998	0.9996	0.9992	0.9984	0.9970	0.9947	0.9911	0.9857
18		1.0000	0.9999	0.9999	0.9997	0.9993	0.9987	0.9976	0.9957	0.9928
19			1.0000	1.0000	0.9999	0.9997	0.9995	0.9989	0.9980	0.9965
20					1.0000	0.9999	0.9998	0.9996	0.9991	0.9984
21						1.0000	0.9999	0.9998	0.9996	0.9993
22							1.0000	0.9999	0.9999	0.9997
23								1.0000	0.9999	0.9999
24									1.0000	1.0000

Table 3 Standard Normal Distribution Cumulative Probabilities

Let Z be a standard normal random variable: $\mu = 0$ and $\sigma = 1$.
 This table contains cumulative probabilities: $P(Z \leq z)$.



z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0002
-3.3	0.0005	0.0005	0.0005	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0003
-3.2	0.0007	0.0007	0.0006	0.0006	0.0006	0.0006	0.0006	0.0005	0.0005	0.0005
-3.1	0.0010	0.0009	0.0009	0.0009	0.0008	0.0008	0.0008	0.0008	0.0007	0.0007
-3.0	0.0013	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
-1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
-1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
-1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
-1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
-1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
-1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
-0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
-0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
-0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
-0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
-0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

Table 3 Standard Normal Distribution Cumulative Probabilities (Continued)

<i>z</i>	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998

Special critical values: $P(Z \geq z_\alpha) = \alpha$

α	0.10	0.05	0.025	0.01	0.005	0.001	0.0005	0.0001
z_α	1.2816	1.6449	1.9600	2.3263	2.5758	3.0902	3.2905	3.7190

α	0.00009	0.00008	0.00007	0.00006	0.00005	0.00004	0.00003	0.00002	0.00001
z_α	3.7455	3.7750	3.8082	3.8461	3.8906	3.9444	4.0128	4.1075	4.2649

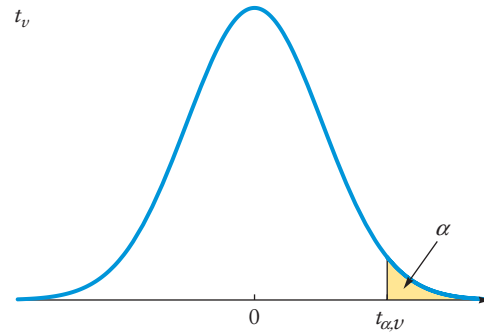
Table 4 Standardized Normal Scores

This table contains the standardized normal scores, z_i , for selected values of n .

i	n					
	10	20	25	30	40	50
1	-1.55	-1.87	-1.96	-2.04	-2.16	-2.24
2	-1.00	-1.40	-1.52	-1.61	-1.75	-1.85
3	-0.66	-1.13	-1.26	-1.36	-1.51	-1.62
4	-0.38	-0.92	-1.06	-1.18	-1.34	-1.46
5	-0.12	-0.74	-0.90	-1.02	-1.20	-1.33
6	0.12	-0.59	-0.76	-0.89	-1.08	-1.22
7	0.38	-0.45	-0.64	-0.78	-0.98	-1.12
8	0.66	-0.31	-0.52	-0.67	-0.88	-1.03
9	1.00	-0.19	-0.41	-0.57	-0.79	-0.95
10	1.55	-0.06	-0.30	-0.47	-0.71	-0.87
11		0.06	-0.20	-0.38	-0.63	-0.80
12		0.19	-0.10	-0.29	-0.56	-0.73
13		0.31	0.00	-0.21	-0.49	-0.67
14		0.45	0.10	-0.12	-0.42	-0.61
15		0.59	0.20	-0.04	-0.35	-0.55
16		0.74	0.30	0.04	-0.28	-0.49
17		0.92	0.41	0.12	-0.22	-0.44
18		1.13	0.52	0.21	-0.16	-0.38
19		1.40	0.64	0.29	-0.09	-0.33
20		1.87	0.76	0.38	-0.03	-0.28
21			0.90	0.47	0.03	-0.23
22			1.06	0.57	0.09	-0.18
23			1.26	0.67	0.16	-0.13
24			1.52	0.78	0.22	-0.07
25			1.96	0.89	0.28	-0.02
26				1.02	0.35	0.02
27				1.18	0.42	0.07
28				1.36	0.49	0.13
29				1.61	0.56	0.18
30				2.04	0.63	0.23
31					0.71	0.28
32					0.79	0.33
33					0.88	0.38
34					0.98	0.44
35					1.08	0.49
36					1.20	0.55
37					1.34	0.61
38					1.51	0.67
39					1.75	0.73
40					2.16	0.80
41						0.87
42						0.95
43						1.03
44						1.12
45						1.22
46						1.33
47						1.46
48						1.62
49						1.85
50						2.24

Table 5 Critical Values for the t Distribution

This table contains critical values associated with the t distribution, $t_{\alpha, \nu}$, defined by α and the degrees of freedom, ν .



ν	α								
	0.20	0.10	0.05	0.025	0.01	0.005	0.001	0.0005	0.0001
1	1.3764	3.0777	6.3138	12.7062	31.8205	63.6567	318.3088	636.6192	3183.0988
2	1.0607	1.8856	2.9200	4.3027	6.9646	9.9248	22.3271	31.5991	70.7001
3	0.9785	1.6377	2.3534	3.1824	4.5407	5.8409	10.2145	12.9240	22.2037
4	0.9410	1.5332	2.1318	2.7764	3.7469	4.6041	7.1732	8.6103	13.0337
5	0.9195	1.4759	2.0150	2.5706	3.3649	4.0321	5.8934	6.8688	9.6776
6	0.9057	1.4398	1.9432	2.4469	3.1427	3.7074	5.2076	5.9588	8.0248
7	0.8960	1.4149	1.8946	2.3646	2.9980	3.4995	4.7853	5.4079	7.0634
8	0.8889	1.3968	1.8595	2.3060	2.8965	3.3554	4.5008	5.0413	6.4420
9	0.8834	1.3830	1.8331	2.2622	2.8214	3.2498	4.2968	4.7809	6.0101
10	0.8791	1.3722	1.8125	2.2281	2.7638	3.1693	4.1437	4.5869	5.6938
11	0.8755	1.3634	1.7959	2.2010	2.7181	3.1058	4.0247	4.4370	5.4528
12	0.8726	1.3562	1.7823	2.1788	2.6810	3.0545	3.9296	4.3178	5.2633
13	0.8702	1.3502	1.7709	2.1604	2.6503	3.0123	3.8520	4.2208	5.1106
14	0.8681	1.3450	1.7613	2.1448	2.6245	2.9768	3.7874	4.1405	4.9850
15	0.8662	1.3406	1.7531	2.1314	2.6025	2.9467	3.7328	4.0728	4.8800
16	0.8647	1.3368	1.7459	2.1199	2.5835	2.9208	3.6862	4.0150	4.7909
17	0.8633	1.3334	1.7396	2.1098	2.5669	2.8982	3.6458	3.9651	4.7144
18	0.8620	1.3304	1.7341	2.1009	2.5524	2.8784	3.6105	3.9216	4.6480
19	0.8610	1.3277	1.7291	2.0930	2.5395	2.8609	3.5794	3.8834	4.5899
20	0.8600	1.3253	1.7247	2.0860	2.5280	2.8453	3.5518	3.8495	4.5385
21	0.8591	1.3232	1.7207	2.0796	2.5176	2.8314	3.5272	3.8193	4.4929
22	0.8583	1.3212	1.7171	2.0739	2.5083	2.8188	3.5050	3.7921	4.4520
23	0.8575	1.3195	1.7139	2.0687	2.4999	2.8073	3.4850	3.7676	4.4152
24	0.8569	1.3178	1.7109	2.0639	2.4922	2.7969	3.4668	3.7454	4.3819
25	0.8562	1.3163	1.7081	2.0595	2.4851	2.7874	3.4502	3.7251	4.3517
26	0.8557	1.3150	1.7056	2.0555	2.4786	2.7787	3.4350	3.7066	4.3240
27	0.8551	1.3137	1.7033	2.0518	2.4727	2.7707	3.4210	3.6896	4.2987
28	0.8546	1.3125	1.7011	2.0484	2.4671	2.7633	3.4082	3.6739	4.2754
29	0.8542	1.3114	1.6991	2.0452	2.4620	2.7564	3.3962	3.6594	4.2539
30	0.8538	1.3104	1.6973	2.0423	2.4573	2.7500	3.3852	3.6460	4.2340
40	0.8507	1.3031	1.6839	2.0211	2.4233	2.7045	3.3069	3.5510	4.0942
50	0.8489	1.2987	1.6759	2.0086	2.4033	2.6778	3.2614	3.4960	4.0140
60	0.8477	1.2958	1.6706	2.0003	2.3901	2.6603	3.2317	3.4602	3.9621
70	0.8468	1.2938	1.6669	1.9944	2.3808	2.6479	3.2108	3.4350	3.9257
80	0.8461	1.2922	1.6641	1.9901	2.3739	2.6387	3.1953	3.4163	3.8988
90	0.8456	1.2910	1.6620	1.9867	2.3685	2.6316	3.1833	3.4019	3.8780
100	0.8452	1.2901	1.6602	1.9840	2.3642	2.6259	3.1737	3.3905	3.8616
200	0.8434	1.2858	1.6525	1.9719	2.3451	2.6006	3.1315	3.3398	3.7891
500	0.8423	1.2832	1.6479	1.9647	2.3338	2.5857	3.1066	3.3101	3.7468
∞	0.8416	1.2816	1.6449	1.9600	2.3263	2.5758	3.0902	3.2905	3.7190

Table 6 Critical Values for the Chi-Square Distribution

This table contains critical values associated with the chi-square distribution, $\chi^2_{\alpha, \nu}$, defined by α and the degrees of freedom, ν .

ν	α							
	0.9999	0.9995	0.999	0.995	0.99	0.975	0.95	0.90
1	0.0 ⁷ 157	0.0 ⁶ 393	0.0 ⁵ 157	0.0 ⁴ 393	0.0002	0.0010	0.0039	0.0158
2	0.0002	0.0010	0.0020	0.0100	0.0201	0.0506	0.1026	0.2107
3	0.0052	0.0153	0.0243	0.0717	0.1148	0.2158	0.3518	0.5844
4	0.0284	0.0639	0.0908	0.2070	0.2971	0.4844	0.7107	1.0636
5	0.0822	0.1581	0.2102	0.4117	0.5543	0.8312	1.1455	1.6103
6	0.1724	0.2994	0.3811	0.6757	0.8721	1.2373	1.6354	2.2041
7	0.3000	0.4849	0.5985	0.9893	1.2390	1.6899	2.1673	2.8331
8	0.4636	0.7104	0.8571	1.3444	1.6465	2.1797	2.7326	3.4895
9	0.6608	0.9717	1.1519	1.7349	2.0879	2.7004	3.3251	4.1682
10	0.8889	1.2650	1.4787	2.1559	2.5582	3.2470	3.9403	4.8652
11	1.1453	1.5868	1.8339	2.6032	3.0535	3.8157	4.5748	5.5778
12	1.4275	1.9344	2.2142	3.0738	3.5706	4.4038	5.2260	6.3038
13	1.7333	2.3051	2.6172	3.5650	4.1069	5.0088	5.8919	7.0415
14	2.0608	2.6967	3.0407	4.0747	4.6604	5.6287	6.5706	7.7895
15	2.4082	3.1075	3.4827	4.6009	5.2293	6.2621	7.2609	8.5468
16	2.7739	3.5358	3.9416	5.1422	5.8122	6.9077	7.9616	9.3122
17	3.1567	3.9802	4.4161	5.6972	6.4078	7.5642	8.6718	10.0852
18	3.5552	4.4394	4.9048	6.2648	7.0149	8.2307	9.3905	10.8649
19	3.9683	4.9123	5.4068	6.8440	7.6327	8.9065	10.1170	11.6509
20	4.3952	5.3981	5.9210	7.4338	8.2604	9.5908	10.8508	12.4426
21	4.8348	5.8957	6.4467	8.0337	8.8972	10.2829	11.5913	13.2396
22	5.2865	6.4045	6.9830	8.6427	9.5425	10.9823	12.3380	14.0415
23	5.7494	6.9237	7.5292	9.2604	10.1957	11.6886	13.0905	14.8480
24	6.2230	7.4527	8.0849	9.8862	10.8564	12.4012	13.8484	15.6587
25	6.7066	7.9910	8.6493	10.5197	11.5240	13.1197	14.6114	16.4734
26	7.1998	8.5379	9.2221	11.1602	12.1981	13.8439	15.3792	17.2919
27	7.7019	9.0932	9.8028	11.8076	12.8785	14.5734	16.1514	18.1139
28	8.2126	9.6563	10.3909	12.4613	13.5647	15.3079	16.9279	18.9392
29	8.7315	10.2268	10.9861	13.1211	14.2565	16.0471	17.7084	19.7677
30	9.2581	10.8044	11.5880	13.7867	14.9535	16.7908	18.4927	20.5992
31	9.7921	11.3887	12.1963	14.4578	15.6555	17.5387	19.2806	21.4336
32	10.3331	11.9794	12.8107	15.1340	16.3622	18.2908	20.0719	22.2706
33	10.8810	12.5763	13.4309	15.8153	17.0735	19.0467	20.8665	23.1102
34	11.4352	13.1791	14.0567	16.5013	17.7891	19.8063	21.6643	23.9523
35	11.9957	13.7875	14.6878	17.1918	18.5089	20.5694	22.4650	24.7967
36	12.5622	14.4012	15.3241	17.8867	19.2327	21.3359	23.2686	25.6433
37	13.1343	15.0202	15.9653	18.5858	19.9602	22.1056	24.0749	26.4921
38	13.7120	15.6441	16.6112	19.2889	20.6914	22.8785	24.8839	27.3430
39	14.2950	16.2729	17.2616	19.9959	21.4262	23.6543	25.6954	28.1958
40	14.8831	16.9062	17.9164	20.7065	22.1643	24.4330	26.5093	29.0505
50	21.0093	23.4610	24.6739	27.9907	29.7067	32.3574	34.7643	37.6886
60	27.4969	30.3405	31.7383	35.5345	37.4849	40.4817	43.1880	46.4589
70	34.2607	37.4674	39.0364	43.2752	45.4417	48.7576	51.7393	55.3289
80	41.2445	44.7910	46.5199	51.1719	53.5401	57.1532	60.3915	64.2778
90	48.4087	52.2758	54.1552	59.1963	61.7541	65.6466	69.1260	73.2911
100	55.7246	59.8957	61.9179	67.3276	70.0649	74.2219	77.9295	82.3581

Table 6 Critical Values for the Chi-Square Distribution (Continued)

ν	α							
	0.10	0.05	0.025	0.01	0.005	0.001	0.0005	0.0001
1	2.7055	3.8415	5.0239	6.6349	7.8794	10.8276	12.1157	15.1367
2	4.6052	5.9915	7.3778	9.2103	10.5966	13.8155	15.2018	18.4207
3	6.2514	7.8147	9.3484	11.3449	12.8382	16.2662	17.7300	21.1075
4	7.7794	9.4877	11.1433	13.2767	14.8603	18.4668	19.9974	23.5127
5	9.2364	11.0705	12.8325	15.0863	16.7496	20.5150	22.1053	25.7448
6	10.6446	12.5916	14.4494	16.8119	18.5476	22.4577	24.1028	27.8563
7	12.0170	14.0671	16.0128	18.4753	20.2777	24.3219	26.0178	29.8775
8	13.3616	15.5073	17.5345	20.0902	21.9550	26.1245	27.8680	31.8276
9	14.6837	16.9190	19.0228	21.6660	23.5894	27.8772	29.6658	33.7199
10	15.9872	18.3070	20.4832	23.2093	25.1882	29.5883	31.4198	35.5640
11	17.2750	19.6751	21.9200	24.7250	26.7568	31.2641	33.1366	37.3670
12	18.5493	21.0261	23.3367	26.2170	28.2995	32.9095	34.8213	39.1344
13	19.8119	22.3620	24.7356	27.6882	29.8195	34.5282	36.4778	40.8707
14	21.0641	23.6848	26.1189	29.1412	31.3193	36.1233	38.1094	42.5793
15	22.3071	24.9958	27.4884	30.5779	32.8013	37.6973	39.7188	44.2632
16	23.5418	26.2962	28.8454	31.9999	34.2672	39.2524	41.3081	45.9249
17	24.7690	27.5871	30.1910	33.4087	35.7185	40.7902	42.8792	47.5664
18	25.9894	28.8693	31.5264	34.8053	37.1565	42.3124	44.4338	49.1894
19	27.2036	30.1435	32.8523	36.1909	38.5823	43.8202	45.9731	50.7955
20	28.4120	31.4104	34.1696	37.5662	39.9968	45.3147	47.4985	52.3860
21	29.6151	32.6706	35.4789	38.9322	41.4011	46.7970	49.0108	53.9620
22	30.8133	33.9244	36.7807	40.2894	42.7957	48.2679	50.5111	55.5246
23	32.0069	35.1725	38.0756	41.6384	44.1813	49.7282	52.0002	57.0746
24	33.1962	36.4150	39.3641	42.9798	45.5585	51.1786	53.4788	58.6130
25	34.3816	37.6525	40.6465	44.3141	46.9279	52.6197	54.9475	60.1403
26	35.5632	38.8851	41.9232	45.6417	48.2899	54.0520	56.4069	61.6573
27	36.7412	40.1133	43.1945	46.9629	49.6449	55.4760	57.8576	63.1645
28	37.9159	41.3371	44.4608	48.2782	50.9934	56.8923	59.3000	64.6624
29	39.0875	42.5570	45.7223	49.5879	52.3356	58.3012	60.7346	66.1517
30	40.2560	43.7730	46.9792	50.8922	53.6720	59.7031	62.1619	67.6326
31	41.4217	44.9853	48.2319	52.1914	55.0027	61.0983	63.5820	69.1057
32	42.5847	46.1943	49.4804	53.4858	56.3281	62.4872	64.9955	70.5712
33	43.7452	47.3999	50.7251	54.7755	57.6484	63.8701	66.4025	72.0296
34	44.9032	48.6024	51.9660	56.0609	58.9639	65.2472	67.8035	73.4812
35	46.0588	49.8018	53.2033	57.3421	60.2748	66.6188	69.1986	74.9262
36	47.2122	50.9985	54.4373	58.6192	61.5812	67.9852	70.5881	76.3650
37	48.3634	52.1923	55.6680	59.8925	62.8833	69.3465	71.9722	77.7977
38	49.5126	53.3835	56.8955	61.1621	64.1814	70.7029	73.3512	79.2247
39	50.6598	54.5722	58.1201	62.4281	65.4756	72.0547	74.7253	80.6462
40	51.8051	55.7585	59.3417	63.6907	66.7660	73.4020	76.0946	82.0623
50	63.1671	67.5048	71.4202	76.1539	79.4900	86.6608	89.5605	95.9687
60	74.3970	79.0819	83.2977	88.3794	91.9517	99.6072	102.6948	109.5029
70	85.5270	90.5312	95.0232	100.4252	104.2149	112.3169	115.5776	122.7547
80	96.5782	101.8795	106.6286	112.3288	116.3211	124.8392	128.2613	135.7825
90	107.5650	113.1453	118.1359	124.1163	128.2989	137.2084	140.7823	148.6273
100	118.4980	124.3421	129.5612	135.8067	140.1695	149.4493	153.1670	161.3187

Table 7 Critical Values for the F Distribution

This table contains critical values associated with the F distribution, F_{α, ν_1, ν_2} , defined by α and the degrees of freedom ν_1 and ν_2 .

$\alpha = 0.05$	ν_1																
ν_2	1	2	3	4	5	6	7	8	9	10	15	20	30	40	50	60	100
1	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54	241.88	245.95	248.01	250.10	251.14	251.77	252.20	253.04
2	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38	19.40	19.43	19.45	19.46	19.47	19.48	19.48	19.49
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.70	8.66	8.62	8.59	8.58	8.57	8.55
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.86	5.80	5.75	5.72	5.70	5.69	5.66
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.62	4.56	4.50	4.46	4.44	4.43	4.41
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	3.94	3.87	3.81	3.77	3.75	3.74	3.71
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.51	3.44	3.38	3.34	3.32	3.30	3.27
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.22	3.15	3.08	3.04	3.02	3.01	2.97
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.01	2.94	2.86	2.83	2.80	2.79	2.76
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.85	2.77	2.70	2.66	2.64	2.62	2.59
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.72	2.65	2.57	2.53	2.51	2.49	2.46
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.62	2.54	2.47	2.43	2.40	2.38	2.35
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.53	2.46	2.38	2.34	2.31	2.30	2.26
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.46	2.39	2.31	2.27	2.24	2.22	2.19
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.40	2.33	2.25	2.20	2.18	2.16	2.12
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.35	2.28	2.19	2.15	2.12	2.11	2.07
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.31	2.23	2.15	2.10	2.08	2.06	2.02
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.27	2.19	2.11	2.06	2.04	2.02	1.98
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.23	2.16	2.07	2.03	2.00	1.98	1.94
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.20	2.12	2.04	1.99	1.97	1.95	1.91
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.18	2.10	2.01	1.96	1.94	1.92	1.88
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.15	2.07	1.98	1.94	1.91	1.89	1.85
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.13	2.05	1.96	1.91	1.88	1.86	1.82
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.11	2.03	1.94	1.89	1.86	1.84	1.80
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.09	2.01	1.92	1.87	1.84	1.82	1.78
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.01	1.93	1.84	1.79	1.76	1.74	1.70
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	1.92	1.84	1.74	1.69	1.66	1.64	1.59
50	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.07	2.03	1.87	1.78	1.69	1.63	1.60	1.58	1.52
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.84	1.75	1.65	1.59	1.56	1.53	1.48
100	3.94	3.09	2.70	2.46	2.31	2.19	2.10	2.03	1.97	1.93	1.77	1.68	1.57	1.52	1.48	1.45	1.39

Table 7 Critical Values for the F Distribution (Continued)

$\alpha = 0.01$	ν_1																
	1	2	3	4	5	6	7	8	9	10	15	20	30	40	50	60	100
2	98.50	99.00	99.17	99.25	99.30	99.33	99.36	99.37	99.39	99.40	99.43	99.45	99.47	99.47	99.48	99.48	99.49
3	34.12	30.82	29.46	28.71	28.24	27.91	27.67	27.49	27.35	27.23	26.87	26.69	26.50	26.41	26.35	26.32	26.24
4	21.20	18.00	16.69	15.98	15.52	15.21	14.98	14.80	14.66	14.55	14.20	14.02	13.84	13.75	13.69	13.65	13.58
5	16.26	13.27	12.06	11.39	10.97	10.67	10.46	10.29	10.16	10.05	9.72	9.55	9.38	9.29	9.24	9.20	9.13
6	13.75	10.92	9.78	9.15	8.75	8.47	8.26	8.10	7.98	7.87	7.56	7.40	7.23	7.14	7.09	7.06	6.99
7	12.25	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72	6.62	6.31	6.16	5.99	5.91	5.86	5.82	5.75
8	11.26	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91	5.81	5.52	5.36	5.20	5.12	5.07	5.03	4.96
9	10.56	8.02	6.99	6.42	6.06	5.80	5.61	5.47	5.35	5.26	4.96	4.81	4.65	4.57	4.52	4.48	4.41
10	10.04	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94	4.85	4.56	4.41	4.25	4.17	4.12	4.08	4.01
11	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.63	4.54	4.25	4.10	3.94	3.86	3.81	3.78	3.71
12	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50	4.39	4.30	4.01	3.86	3.70	3.62	3.57	3.54	3.47
13	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.19	4.10	3.82	3.66	3.51	3.43	3.38	3.34	3.27
14	8.86	6.51	5.56	5.04	4.69	4.46	4.28	4.14	4.03	3.94	3.66	3.51	3.35	3.27	3.22	3.18	3.11
15	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89	3.80	3.52	3.37	3.21	3.13	3.08	3.05	2.98
16	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78	3.69	3.41	3.26	3.10	3.02	2.97	2.93	2.86
17	8.40	6.11	5.18	4.67	4.34	4.10	3.93	3.79	3.68	3.59	3.31	3.16	3.00	2.92	2.87	2.83	2.76
18	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60	3.51	3.23	3.08	2.92	2.84	2.78	2.75	2.68
19	8.18	5.93	5.01	4.50	4.17	3.94	3.77	3.63	3.52	3.43	3.15	3.00	2.84	2.76	2.71	2.67	2.60
20	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46	3.37	3.09	2.94	2.78	2.69	2.64	2.61	2.54
21	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40	3.31	3.03	2.88	2.72	2.64	2.58	2.55	2.48
22	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35	3.26	2.98	2.83	2.67	2.58	2.53	2.50	2.42
23	7.88	5.66	4.76	4.26	3.94	3.71	3.54	3.41	3.30	3.21	2.93	2.78	2.62	2.54	2.48	2.45	2.37
24	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26	3.17	2.89	2.74	2.58	2.49	2.44	2.40	2.33
25	7.77	5.57	4.68	4.18	3.85	3.63	3.46	3.32	3.22	3.13	2.85	2.70	2.54	2.45	2.40	2.36	2.29
30	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07	2.98	2.70	2.55	2.39	2.30	2.25	2.21	2.13
40	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89	2.80	2.52	2.37	2.20	2.11	2.06	2.02	1.94
50	7.17	5.06	4.20	3.72	3.41	3.19	3.02	2.89	2.78	2.70	2.42	2.27	2.10	2.01	1.95	1.91	1.82
60	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72	2.63	2.35	2.20	2.03	1.94	1.88	1.84	1.75
100	6.90	4.82	3.98	3.51	3.21	2.99	2.82	2.69	2.59	2.50	2.22	2.07	1.89	1.80	1.74	1.69	1.60

Table 7 Critical Values for the F Distribution (Continued)

$\alpha = 0.001$		ν_1															
ν_2	1	2	3	4	5	6	7	8	9	10	15	20	30	40	50	60	100
2	998.50	999.00	999.17	999.25	999.30	999.33	999.36	999.37	999.39	999.40	999.43	999.45	999.47	999.47	999.48	999.48	999.49
3	167.03	148.50	141.11	137.10	134.58	132.85	131.58	130.62	129.86	129.25	127.37	126.42	125.45	124.96	124.66	124.47	124.07
4	74.14	61.25	56.18	53.44	51.71	50.53	49.66	49.00	48.47	48.05	46.76	46.10	45.43	45.09	44.88	44.75	44.47
5	47.18	37.12	33.20	31.09	29.75	28.83	28.16	27.65	27.24	26.92	25.91	25.39	24.87	24.60	24.44	24.33	24.12
6	35.51	27.00	23.70	21.92	20.80	20.03	19.46	19.03	18.69	18.41	17.56	17.12	16.67	16.44	16.31	16.21	16.03
7	29.25	21.69	18.77	17.20	16.21	15.52	15.02	14.63	14.33	14.08	13.32	12.93	12.53	12.33	12.20	12.12	11.95
8	25.41	18.49	15.83	14.39	13.48	12.86	12.40	12.05	11.77	11.54	10.84	10.48	10.11	9.92	9.80	9.73	9.57
9	22.86	16.39	13.90	12.56	11.71	11.13	10.70	10.37	10.11	9.89	9.24	8.90	8.55	8.37	8.26	8.19	8.04
10	21.04	14.91	12.55	11.28	10.48	9.93	9.52	9.20	8.96	8.75	8.13	7.80	7.47	7.30	7.19	7.12	6.98
11	19.69	13.81	11.56	10.35	9.58	9.05	8.66	8.35	8.12	7.92	7.32	7.01	6.68	6.52	6.42	6.35	6.21
12	18.64	12.97	10.80	9.63	8.89	8.38	8.00	7.71	7.48	7.29	6.71	6.40	6.09	5.93	5.83	5.76	5.63
13	17.82	12.31	10.21	9.07	8.35	7.86	7.49	7.21	6.98	6.80	6.23	5.93	5.63	5.47	5.37	5.30	5.17
14	17.14	11.78	9.73	8.62	7.92	7.44	7.08	6.80	6.58	6.40	5.85	5.56	5.25	5.10	5.00	4.94	4.81
15	16.59	11.34	9.34	8.25	7.57	7.09	6.74	6.47	6.26	6.08	5.54	5.25	4.95	4.80	4.70	4.64	4.51
16	16.12	10.97	9.01	7.94	7.27	6.80	6.46	6.19	5.98	5.81	5.27	4.99	4.70	4.54	4.45	4.39	4.26
17	15.72	10.66	8.73	7.68	7.02	6.56	6.22	5.96	5.75	5.58	5.05	4.78	4.48	4.33	4.24	4.18	4.05
18	15.38	10.39	8.49	7.46	6.81	6.35	6.02	5.76	5.56	5.39	4.87	4.59	4.30	4.15	4.06	4.00	3.87
19	15.08	10.16	8.28	7.27	6.62	6.18	5.85	5.59	5.39	5.22	4.70	4.43	4.14	3.99	3.90	3.84	3.71
20	14.82	9.95	8.10	7.10	6.46	6.02	5.69	5.44	5.24	5.08	4.56	4.29	4.00	3.86	3.77	3.70	3.58
21	14.59	9.77	7.94	6.95	6.32	5.88	5.56	5.31	5.11	4.95	4.44	4.17	3.88	3.74	3.64	3.58	3.46
22	14.38	9.61	7.80	6.81	6.19	5.76	5.44	5.19	4.99	4.83	4.33	4.06	3.78	3.63	3.54	3.48	3.35
23	14.20	9.47	7.67	6.70	6.08	5.65	5.33	5.09	4.89	4.73	4.23	3.96	3.68	3.53	3.44	3.38	3.25
24	14.03	9.34	7.55	6.59	5.98	5.55	5.23	4.99	4.80	4.64	4.14	3.87	3.59	3.45	3.36	3.29	3.17
25	13.88	9.22	7.45	6.49	5.89	5.46	5.15	4.91	4.71	4.56	4.06	3.79	3.52	3.37	3.28	3.22	3.09
30	13.29	8.77	7.05	6.12	5.53	5.12	4.82	4.58	4.39	4.24	3.75	3.49	3.22	3.07	2.98	2.92	2.79
40	12.61	8.25	6.59	5.70	5.13	4.73	4.44	4.21	4.02	3.87	3.40	3.14	2.87	2.73	2.64	2.57	2.44
50	12.22	7.96	6.34	5.46	4.90	4.51	4.22	4.00	3.82	3.67	3.20	2.95	2.68	2.53	2.44	2.38	2.25
60	11.97	7.77	6.17	5.31	4.76	4.37	4.09	3.86	3.69	3.54	3.08	2.83	2.55	2.41	2.32	2.25	2.12
100	11.50	7.41	5.86	5.02	4.48	4.11	3.83	3.61	3.44	3.30	2.84	2.59	2.32	2.17	2.08	2.01	1.87

Table 8 Critical Values for the Studentized Range Distribution

This table contains critical values associated with the Studentized range distribution, $Q_{\alpha, k, \nu}$, defined by α , and the degrees of freedom k and ν , where k is the number of degrees of freedom in the numerator (the number of treatment groups) and ν is the number of degrees of freedom in the denominator.

ν	k																			
	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	
2	6.085	8.331	9.798	10.881	11.734	12.434	13.027	13.538	13.987	14.387	14.747	15.076	15.375	15.650	15.905	16.143	16.365	16.573	16.769	
3	4.501	5.910	6.825	7.502	8.037	8.478	8.852	9.177	9.462	9.717	9.946	10.155	10.346	10.522	10.686	10.838	10.980	11.114	11.240	
4	3.926	5.040	5.757	6.287	6.706	7.053	7.347	7.602	7.826	8.027	8.208	8.373	8.524	8.664	8.793	8.914	9.027	9.133	9.233	
5	3.635	4.602	5.218	5.673	6.033	6.330	6.582	6.801	6.995	7.167	7.324	7.465	7.596	7.716	7.828	7.932	8.030	8.122	8.208	
6	3.460	4.339	4.896	5.305	5.629	5.895	6.122	6.319	6.493	6.649	6.789	6.917	7.034	7.143	7.244	7.338	7.426	7.509	7.587	
7	3.344	4.165	4.681	5.060	5.359	5.606	5.815	5.997	6.158	6.302	6.431	6.550	6.658	6.759	6.852	6.939	7.020	7.097	7.169	
8	3.261	4.041	4.529	4.886	5.167	5.399	5.596	5.767	5.918	6.053	6.175	6.287	6.389	6.483	6.571	6.653	6.729	6.801	6.870	
9	3.199	3.948	4.415	4.755	5.024	5.244	5.432	5.595	5.738	5.867	5.983	6.089	6.186	6.276	6.359	6.437	6.510	6.579	6.644	
10	3.151	3.877	4.327	4.654	4.912	5.124	5.304	5.460	5.598	5.722	5.833	5.935	6.028	6.114	6.194	6.269	6.339	6.405	6.467	
11	3.113	3.820	4.256	4.574	4.823	5.028	5.202	5.353	5.486	5.605	5.713	5.811	5.901	5.984	6.062	6.134	6.202	6.265	6.325	
12	3.081	3.773	4.199	4.508	4.750	4.950	5.119	5.265	5.395	5.510	5.615	5.710	5.797	5.878	5.953	6.023	6.089	6.151	6.209	
13	3.055	3.734	4.151	4.453	4.690	4.884	5.049	5.192	5.318	5.431	5.533	5.625	5.711	5.789	5.862	5.931	5.995	6.055	6.112	
14	3.033	3.701	4.111	4.407	4.639	4.829	4.990	5.130	5.253	5.363	5.463	5.554	5.637	5.714	5.785	5.852	5.915	5.973	6.029	
15	3.014	3.673	4.076	4.367	4.595	4.782	4.940	5.077	5.198	5.306	5.403	5.492	5.574	5.649	5.719	5.785	5.846	5.904	5.958	
16	2.998	3.649	4.046	4.333	4.557	4.741	4.896	5.031	5.150	5.256	5.352	5.439	5.519	5.593	5.662	5.726	5.786	5.843	5.896	
17	2.984	3.628	4.020	4.303	4.524	4.705	4.858	4.991	5.108	5.212	5.306	5.392	5.471	5.544	5.612	5.675	5.734	5.790	5.842	
18	2.971	3.609	3.997	4.276	4.494	4.673	4.824	4.955	5.071	5.173	5.266	5.351	5.429	5.501	5.567	5.629	5.688	5.743	5.794	
19	2.960	3.593	3.977	4.253	4.468	4.645	4.794	4.924	5.037	5.139	5.231	5.314	5.391	5.462	5.528	5.589	5.647	5.701	5.752	
20	2.950	3.578	3.958	4.232	4.445	4.620	4.768	4.895	5.008	5.108	5.199	5.282	5.357	5.427	5.492	5.553	5.610	5.663	5.714	
25	2.913	3.523	3.890	4.153	4.358	4.526	4.667	4.789	4.897	4.993	5.079	5.158	5.230	5.297	5.359	5.417	5.471	5.522	5.570	
30	2.888	3.487	3.845	4.102	4.301	4.464	4.601	4.720	4.824	4.917	5.001	5.077	5.147	5.211	5.271	5.327	5.379	5.429	5.475	
40	2.858	3.442	3.791	4.039	4.232	4.388	4.521	4.634	4.735	4.824	4.904	4.977	5.044	5.106	5.163	5.216	5.266	5.313	5.358	
50	2.841	3.416	3.758	4.002	4.190	4.344	4.473	4.584	4.681	4.768	4.847	4.918	4.983	5.043	5.098	5.150	5.199	5.245	5.288	
100	2.806	3.365	3.695	3.929	4.109	4.256	4.379	4.484	4.577	4.659	4.733	4.800	4.862	4.918	4.971	5.020	5.066	5.108	5.149	
200	2.789	3.339	3.664	3.893	4.069	4.212	4.332	4.435	4.525	4.605	4.677	4.742	4.802	4.857	4.908	4.955	4.999	5.041	5.080	
300	2.783	3.331	3.654	3.881	4.056	4.198	4.317	4.419	4.508	4.587	4.659	4.723	4.782	4.837	4.887	4.934	4.978	5.019	5.057	
400	2.780	3.327	3.649	3.875	4.050	4.191	4.309	4.411	4.500	4.578	4.649	4.714	4.772	4.826	4.876	4.923	4.967	5.007	5.046	
500	2.779	3.324	3.645	3.872	4.046	4.187	4.305	4.406	4.494	4.573	4.644	4.708	4.766	4.820	4.870	4.917	4.960	5.001	5.039	

Table 8 Critical Values for the Studentized Range Distribution (Continued)

ν	k																			
	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	
2	14.035	19.019	22.293	24.717	26.628	28.199	29.528	30.677	31.687	32.585	33.395	34.129	34.802	35.421	35.995	36.529	37.028	37.496	37.937	
3	8.260	10.616	12.169	13.324	14.240	14.997	15.640	16.198	16.689	17.128	17.524	17.884	18.214	18.519	18.802	19.065	19.311	19.543	19.761	
4	6.511	8.118	9.173	9.958	10.582	11.099	11.539	11.925	12.264	12.566	12.840	13.089	13.318	13.530	13.726	13.909	14.081	14.242	14.394	
5	5.702	6.976	7.806	8.421	8.913	9.321	9.669	9.971	10.239	10.479	10.695	10.893	11.075	11.243	11.399	11.544	11.681	11.809	11.930	
6	5.243	6.331	7.033	7.556	7.974	8.318	8.611	8.869	9.097	9.300	9.485	9.653	9.808	9.951	10.084	10.208	10.325	10.434	10.538	
7	4.948	5.919	6.543	7.006	7.373	7.678	7.940	8.167	8.368	8.548	8.711	8.859	8.996	9.124	9.242	9.353	9.456	9.553	9.645	
8	4.745	5.635	6.204	6.625	6.960	7.238	7.475	7.681	7.864	8.028	8.177	8.312	8.437	8.552	8.659	8.760	8.854	8.942	9.026	
9	4.595	5.428	5.957	6.347	6.658	6.915	7.134	7.326	7.495	7.647	7.785	7.910	8.026	8.133	8.233	8.326	8.413	8.495	8.573	
10	4.482	5.270	5.769	6.136	6.428	6.669	6.875	7.055	7.214	7.356	7.485	7.603	7.712	7.813	7.906	7.994	8.076	8.153	8.226	
11	4.392	5.146	5.621	5.970	6.247	6.476	6.671	6.842	6.992	7.127	7.250	7.362	7.465	7.560	7.649	7.732	7.810	7.883	7.952	
12	4.320	5.046	5.502	5.836	6.101	6.321	6.507	6.670	6.814	6.943	7.060	7.167	7.265	7.356	7.441	7.520	7.594	7.664	7.731	
13	4.261	4.964	5.404	5.727	5.981	6.192	6.372	6.528	6.666	6.791	6.903	7.006	7.100	7.188	7.269	7.345	7.417	7.484	7.548	
14	4.210	4.895	5.322	5.634	5.881	6.085	6.258	6.409	6.543	6.664	6.772	6.871	6.962	7.047	7.125	7.199	7.268	7.333	7.394	
15	4.167	4.836	5.252	5.556	5.796	5.994	6.162	6.309	6.438	6.555	6.660	6.757	6.845	6.927	7.003	7.074	7.141	7.204	7.264	
16	4.131	4.786	5.192	5.488	5.722	5.915	6.079	6.222	6.348	6.461	6.564	6.658	6.743	6.824	6.897	6.967	7.032	7.093	7.151	
17	4.099	4.742	5.140	5.430	5.659	5.847	6.007	6.147	6.270	6.380	6.480	6.572	6.656	6.733	6.806	6.873	6.937	6.997	7.053	
18	4.071	4.703	5.094	5.379	5.603	5.787	5.944	6.081	6.201	6.309	6.407	6.496	6.579	6.655	6.725	6.791	6.854	6.912	6.967	
19	4.046	4.669	5.054	5.333	5.553	5.735	5.888	6.022	6.141	6.246	6.342	6.430	6.510	6.585	6.654	6.719	6.780	6.837	6.891	
20	4.024	4.639	5.018	5.293	5.509	5.687	5.839	5.970	6.086	6.190	6.285	6.370	6.449	6.523	6.591	6.654	6.714	6.770	6.823	
25	3.942	4.527	4.884	5.143	5.346	5.513	5.654	5.777	5.885	5.982	6.070	6.150	6.223	6.291	6.355	6.414	6.469	6.521	6.571	
30	3.889	4.454	4.799	5.048	5.242	5.401	5.536	5.653	5.756	5.848	5.932	6.008	6.078	6.142	6.202	6.258	6.311	6.360	6.407	
40	3.825	4.367	4.695	4.931	5.114	5.265	5.392	5.502	5.599	5.685	5.764	5.835	5.900	5.961	6.017	6.069	6.118	6.165	6.208	
50	3.787	4.316	4.634	4.863	5.040	5.185	5.308	5.414	5.507	5.590	5.665	5.734	5.796	5.854	5.908	5.958	6.005	6.050	6.092	
100	3.714	4.216	4.516	4.730	4.896	5.031	5.144	5.242	5.328	5.405	5.474	5.537	5.594	5.648	5.697	5.743	5.786	5.826	5.864	
200	3.714	4.216	4.516	4.730	4.896	5.031	5.144	5.242	5.328	5.405	5.474	5.537	5.594	5.648	5.697	5.743	5.786	5.826	5.864	
300	3.666	4.152	4.440	4.645	4.803	4.931	5.039	5.132	5.213	5.286	5.351	5.410	5.464	5.514	5.560	5.603	5.644	5.682	5.717	
400	3.661	4.144	4.431	4.634	4.791	4.919	5.026	5.118	5.199	5.271	5.335	5.394	5.448	5.498	5.543	5.586	5.626	5.664	5.699	
500	3.657	4.139	4.425	4.628	4.784	4.911	5.018	5.110	5.190	5.262	5.327	5.385	5.438	5.488	5.533	5.576	5.616	5.653	5.688	

Table 8 Critical Values for the Studentized Range Distribution (Continued)

$\alpha = 0.001$	k																			
	ν	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
2	44.666	60.323	70.586	78.162	84.127	89.022	93.650	97.285	100.480	103.325	105.886	108.211	110.340	112.300	114.115	115.805	117.385	118.867	120.263	121.600
3	18.275	23.298	26.609	29.075	31.030	32.645	34.016	35.327	36.389	37.338	38.194	38.974	39.688	40.347	40.959	41.529	42.062	42.564	43.036	43.478
4	12.174	14.965	16.798	18.225	19.333	20.253	21.037	21.719	22.323	22.862	23.350	23.795	24.204	24.581	24.932	25.259	25.566	25.854	26.126	26.383
5	9.710	11.671	12.959	13.924	14.695	15.335	15.882	16.358	16.780	17.158	17.500	17.811	18.098	18.402	18.651	18.884	19.102	19.307	19.501	19.684
6	8.431	9.955	10.965	11.719	12.322	12.824	13.254	13.629	13.961	14.260	14.530	14.777	15.004	15.215	15.411	15.593	15.765	15.927	16.079	16.223
7	7.649	8.933	9.761	10.388	10.883	11.316	11.674	11.988	12.265	12.515	12.742	12.949	13.139	13.316	13.480	13.634	13.778	13.914	14.043	14.166
8	7.130	8.252	8.980	9.523	9.948	10.317	10.625	10.894	11.133	11.347	11.559	11.740	11.906	12.060	12.203	12.337	12.463	12.582	12.694	12.801
9	7.130	8.252	8.980	9.523	9.948	10.317	10.625	10.894	11.133	11.347	11.559	11.740	11.906	12.060	12.203	12.337	12.463	12.582	12.694	12.801
10	6.486	7.411	8.007	8.451	8.805	9.100	9.353	9.574	9.770	9.954	10.106	10.245	10.387	10.512	10.629	10.737	10.840	10.936	11.027	11.113
11	6.274	7.137	7.688	8.099	8.427	8.700	8.934	9.138	9.320	9.483	9.631	9.767	9.892	10.017	10.121	10.218	10.309	10.394	10.475	10.552
12	6.106	6.917	7.442	7.820	8.128	8.383	8.602	8.793	8.963	9.116	9.254	9.381	9.498	9.607	9.708	9.803	9.892	9.976	10.055	10.129
13	5.969	6.740	7.234	7.595	7.885	8.126	8.333	8.513	8.674	8.818	8.949	9.068	9.179	9.281	9.377	9.466	9.550	9.630	9.705	9.776
14	5.855	6.593	7.070	7.410	7.692	7.914	8.111	8.282	8.434	8.571	8.696	8.810	8.915	9.012	9.103	9.188	9.268	9.343	9.414	9.481
15	5.760	6.470	6.920	7.257	7.517	7.742	7.924	8.088	8.234	8.365	8.483	8.592	8.693	8.786	8.873	8.954	9.030	9.102	9.170	9.234
16	5.678	6.365	6.799	7.125	7.377	7.585	7.769	7.923	8.063	8.189	8.303	8.407	8.504	8.593	8.676	8.754	8.828	8.897	8.963	9.025
17	5.614	6.274	6.695	7.010	7.254	7.457	7.629	7.783	7.921	8.037	8.147	8.248	8.341	8.427	8.508	8.583	8.654	8.720	8.783	8.843
18	5.550	6.201	6.609	6.909	7.147	7.343	7.511	7.658	7.781	7.908	8.017	8.116	8.199	8.283	8.361	8.433	8.502	8.566	8.628	8.687
19	5.493	6.129	6.527	6.820	7.051	7.243	7.407	7.550	7.676	7.790	7.894	7.990	8.079	8.162	8.238	8.302	8.369	8.431	8.491	8.548
20	5.444	6.065	6.455	6.741	6.967	7.154	7.314	7.453	7.577	7.687	7.788	7.880	7.966	8.046	8.121	8.190	8.256	8.318	8.376	8.431
25	5.264	5.840	6.196	6.456	6.662	6.831	6.976	7.102	7.213	7.314	7.404	7.487	7.558	7.629	7.696	7.758	7.816	7.871	7.924	7.974
30	5.154	5.698	6.033	6.277	6.469	6.628	6.763	6.880	6.984	7.077	7.161	7.238	7.309	7.375	7.436	7.494	7.548	7.598	7.646	7.692
40	5.022	5.527	5.837	6.062	6.239	6.385	6.508	6.615	6.710	6.795	6.872	6.942	7.006	7.066	7.121	7.173	7.222	7.268	7.312	7.354
50	4.946	5.426	5.725	5.939	6.107	6.245	6.361	6.463	6.552	6.632	6.705	6.771	6.832	6.888	6.940	6.989	7.035	7.078	7.119	7.159
100	4.795	5.244	5.512	5.706	5.855	5.978	6.083	6.173	6.252	6.323	6.387	6.445	6.499	6.548	6.594	6.637	6.678	6.715	6.751	6.786
200	4.723	5.151	5.408	5.596	5.738	5.854	5.952	6.038	6.110	6.178	6.237	6.292	6.342	6.388	6.431	6.471	6.509	6.544	6.577	6.610
300	4.700	5.122	5.375	5.556	5.696	5.814	5.910	5.993	6.066	6.131	6.189	6.244	6.291	6.335	6.379	6.418	6.455	6.489	6.522	6.554
400	4.688	5.107	5.358	5.538	5.677	5.791	5.890	5.972	6.044	6.108	6.166	6.219	6.267	6.312	6.355	6.393	6.427	6.460	6.494	6.526
500	4.681	5.098	5.348	5.527	5.665	5.778	5.874	5.959	6.031	6.095	6.152	6.205	6.253	6.297	6.338	6.376	6.412	6.448	6.483	6.517

Table 9 Critical Values for the Wilcoxon Signed-Rank Statistic

This table contains critical values and probabilities for the Wilcoxon signed-rank statistic T_+ : n is the sample size, and c_1 and c_2 are defined by $P(T_+ \leq c_1) = \alpha$ and $P(T_+ \geq c_2) = \alpha$, respectively.

n	c_1	c_2	α	n	c_1	c_2	α	n	c_1	c_2	α	n	c_1	c_2	α				
1	0	1	0.5000	10	0	55	0.0010	12	0	78	0.0002	13	0	91	0.0001	14	0	105	0.0001
2	0	3	0.2500		1	54	0.0020		1	77	0.0005		1	90	0.0002		1	104	0.0001
3	0	6	0.1250		2	53	0.0029		2	76	0.0007		2	89	0.0004		2	103	0.0002
4	0	10	0.0625		3	52	0.0049		3	75	0.0012		3	88	0.0006		3	102	0.0003
	1	9	0.1250		4	51	0.0068		4	74	0.0017		4	87	0.0009		4	101	0.0004
5	0	15	0.0313		5	50	0.0098		5	73	0.0024		5	86	0.0012		5	100	0.0006
	1	14	0.0625		6	49	0.0137		6	72	0.0034		6	85	0.0017		6	99	0.0009
	2	13	0.0938		7	48	0.0186		7	71	0.0046		7	84	0.0023		7	98	0.0012
	3	12	0.1563		8	47	0.0244		8	70	0.0061		8	83	0.0031		8	97	0.0015
6	0	21	0.0156		9	46	0.0322		9	69	0.0081		9	82	0.0040		9	96	0.0020
	1	20	0.0313		10	45	0.0420		10	68	0.0105		10	81	0.0052		10	95	0.0026
	2	19	0.0469		11	44	0.0527		11	67	0.0134		11	80	0.0067		11	94	0.0034
	3	18	0.0781		12	43	0.0654		12	66	0.0171		12	79	0.0085		12	93	0.0043
	4	17	0.1094		13	42	0.0801		13	65	0.0212		13	78	0.0107		13	92	0.0054
7	0	28	0.0078		14	41	0.0967		14	64	0.0261		14	77	0.0133		14	91	0.0067
	1	27	0.0156		15	40	0.1162		15	63	0.0320		15	76	0.0164		15	90	0.0083
	2	26	0.0234	16	39	0.1377	16	62	0.0386	16	75	0.0199	16	89	0.0101				
	3	25	0.0391	11	0	66	0.0005	17	61	0.0461	17	74	0.0239	17	88	0.0123			
	4	24	0.0547		1	65	0.0010	18	60	0.0549	18	73	0.0287	18	87	0.0148			
	5	23	0.0781		2	64	0.0015	19	59	0.0647	19	72	0.0341	19	86	0.0176			
	6	22	0.1094		3	63	0.0024	20	58	0.0757	20	71	0.0402	20	85	0.0209			
7	21	0.1484	4		62	0.0034	21	57	0.0881	21	70	0.0471	21	84	0.0247				
8	0	36	0.0039		5	61	0.0049	22	56	0.1018	22	69	0.0549	22	83	0.0290			
	1	35	0.0078		6	60	0.0068	23	55	0.1167	23	68	0.0636	23	82	0.0338			
	2	34	0.0117	7	59	0.0093	24	54	0.1331	24	67	0.0732	24	81	0.0392				
	3	33	0.0195	8	58	0.0122	12	25	53	0.1506	25	66	0.0839	25	80	0.0453			
	4	32	0.0273	9	57	0.0161		26	65	0.0955	26	65	0.0955	26	79	0.0520			
	5	31	0.0391	10	56	0.0210		27	64	0.1082	27	64	0.1082	27	78	0.0594			
	6	30	0.0547	11	55	0.0269		28	63	0.1219	28	63	0.1219	28	77	0.0676			
	7	29	0.0742	12	54	0.0337		29	62	0.1367	29	62	0.1367	29	76	0.0765			
8	28	0.0977	13	53	0.0415	30		61	0.1527	30	61	0.1527	30	75	0.0863				
9	27	0.1250	14	52	0.0508	13				31	74	0.0969	31	74	0.0969				
9	0	45	0.0020	15	51					0.0615	32	73	0.1083	32	73	0.1083			
	1	44	0.0039	16	50		0.0737			33	72	0.1206	33	72	0.1206				
	2	43	0.0059	17	49		0.0874			34	71	0.1338	34	71	0.1338				
	3	42	0.0098	18	48		0.1030			35	70	0.1479	35	70	0.1479				
	4	41	0.0137	19	47		0.1201			36	69	0.1629	36	69	0.1629				
	5	40	0.0195	20	46		0.1392												
	6	39	0.0273																
	7	38	0.0371																
	8	37	0.0488																
	9	36	0.0645																
	10	35	0.0820																
	11	34	0.1016																
12	33	0.1250																	

Table 9 Critical Values for the Wilcoxon Signed-Rank Statistic (Continued)

n	c_1	c_2	α	n	c_1	c_2	α	n	c_1	c_2	α	n	c_1	c_2	α
15	0	120	0.0000	16	0	136	0.0000	17	0	153	0.0000	18	0	171	0.0000
	1	119	0.0001		1	135	0.0000		1	152	0.0000		1	170	0.0000
	2	118	0.0001		2	134	0.0000		2	151	0.0000		2	169	0.0000
	3	117	0.0002		3	133	0.0001		3	150	0.0000		3	168	0.0000
	4	116	0.0002		4	132	0.0001		4	149	0.0001		4	167	0.0000
	5	115	0.0003		5	131	0.0002		5	148	0.0001		5	166	0.0000
	6	114	0.0004		6	130	0.0002		6	147	0.0001		6	165	0.0001
	7	113	0.0006		7	129	0.0003		7	146	0.0001		7	164	0.0001
	8	112	0.0008		8	128	0.0004		8	145	0.0002		8	163	0.0001
	9	111	0.0010		9	127	0.0005		9	144	0.0003		9	162	0.0001
	10	110	0.0013		10	126	0.0007		10	143	0.0003		10	161	0.0002
	11	109	0.0017		11	125	0.0008		11	142	0.0004		11	160	0.0002
	12	108	0.0021		12	124	0.0011		12	141	0.0005		12	159	0.0003
	13	107	0.0027		13	123	0.0013		13	140	0.0007		13	158	0.0003
	14	106	0.0034		14	122	0.0017		14	139	0.0008		14	157	0.0004
	15	105	0.0042		15	121	0.0021		15	138	0.0010		15	156	0.0005
	16	104	0.0051		16	120	0.0026		16	137	0.0013		16	155	0.0006
	17	103	0.0062		17	119	0.0031		17	136	0.0016		17	154	0.0008
	18	102	0.0075		18	118	0.0038		18	135	0.0019		18	153	0.0010
	19	101	0.0090		19	117	0.0046		19	134	0.0023		19	152	0.0012
	20	100	0.0108		20	116	0.0055		20	133	0.0028		20	151	0.0014
	21	99	0.0128		21	115	0.0065		21	132	0.0033		21	150	0.0017
	22	98	0.0151		22	114	0.0078		22	131	0.0040		22	149	0.0020
	23	97	0.0177		23	113	0.0091		23	130	0.0047		23	148	0.0024
	24	96	0.0206		24	112	0.0107		24	129	0.0055		24	147	0.0028
	25	95	0.0240		25	111	0.0125		25	128	0.0064		25	146	0.0033
	26	94	0.0277		26	110	0.0145		26	127	0.0075		26	145	0.0038
	27	93	0.0319		27	109	0.0168		27	126	0.0087		27	144	0.0045
	28	92	0.0365		28	108	0.0193		28	125	0.0101		28	143	0.0052
	29	91	0.0416		29	107	0.0222		29	124	0.0116		29	142	0.0060
	30	90	0.0473		30	106	0.0253		30	123	0.0133		30	141	0.0069
	31	89	0.0535		31	105	0.0288		31	122	0.0153		31	140	0.0080
	32	88	0.0603		32	104	0.0327		32	121	0.0174		32	139	0.0091
	33	87	0.0677		33	103	0.0370		33	120	0.0198		33	138	0.0104
	34	86	0.0757		34	102	0.0416		34	119	0.0224		34	137	0.0118
	35	85	0.0844		35	101	0.0467		35	118	0.0253		35	136	0.0134
	36	84	0.0938		36	100	0.0523		36	117	0.0284		36	135	0.0152
	37	83	0.1039		37	99	0.0583		37	116	0.0319		37	134	0.0171
	38	82	0.1147		38	98	0.0649		38	115	0.0357		38	133	0.0192
	39	81	0.1262		39	97	0.0719		39	114	0.0398		39	132	0.0216
	40	80	0.1384		40	96	0.0795		40	113	0.0443		40	131	0.0241
	41	79	0.1514		41	95	0.0877		41	112	0.0492		41	130	0.0269
					42	94	0.0964		42	111	0.0544		42	129	0.0300
					43	93	0.1057		43	110	0.0601		43	128	0.0333
					44	92	0.1156		44	109	0.0662		44	127	0.0368
					45	91	0.1261		45	108	0.0727		45	126	0.0407
					46	90	0.1372		46	107	0.0797		46	125	0.0449
					47	89	0.1489		47	106	0.0871		47	124	0.0494
									48	105	0.0950		48	123	0.0542
									49	104	0.1034		49	122	0.0594
									50	103	0.1123		50	121	0.0649
									51	102	0.1217		51	120	0.0708
									52	101	0.1317		52	119	0.0770
									53	100	0.1421		53	118	0.0837
									54	99	0.1530		54	117	0.0907
													55	116	0.0982
													56	115	0.1061
													57	114	0.1144
													58	113	0.1231
													59	112	0.1323
													60	111	0.1419
													61	110	0.1519

Table 9 Critical Values for the Wilcoxon Signed-Rank Statistic (Continued)

n	c_1	c_2	α	n	c_1	c_2	α	n	c_1	c_2	α	n	c_1	c_2	α
19	0	190	0.0000	19	41	149	0.0145	20	0	210	0.0000	20	41	169	0.0077
	1	189	0.0000		42	148	0.0162		1	209	0.0000		42	168	0.0086
	2	188	0.0000		43	147	0.0180		2	208	0.0000		43	167	0.0096
	3	187	0.0000		44	146	0.0201		3	207	0.0000		44	166	0.0107
	4	186	0.0000		45	145	0.0223		4	206	0.0000		45	165	0.0120
	5	185	0.0000		46	144	0.0247		5	205	0.0000		46	164	0.0133
	6	184	0.0000		47	143	0.0273		6	204	0.0000		47	163	0.0148
	7	183	0.0000		48	142	0.0301		7	203	0.0000		48	162	0.0164
	8	182	0.0000		49	141	0.0331		8	202	0.0000		49	161	0.0181
	9	181	0.0001		50	140	0.0364		9	201	0.0000		50	160	0.0200
	10	180	0.0001		51	139	0.0399		10	200	0.0000		51	159	0.0220
	11	179	0.0001		52	138	0.0437		11	199	0.0001		52	158	0.0242
	12	178	0.0001		53	137	0.0478		12	198	0.0001		53	157	0.0266
	13	177	0.0002		54	136	0.0521		13	197	0.0001		54	156	0.0291
	14	176	0.0002		55	135	0.0567		14	196	0.0001		55	155	0.0319
	15	175	0.0003		56	134	0.0616		15	195	0.0001		56	154	0.0348
	16	174	0.0003		57	133	0.0668		16	194	0.0002		57	153	0.0379
	17	173	0.0004		58	132	0.0723		17	193	0.0002		58	152	0.0413
	18	172	0.0005		59	131	0.0782		18	192	0.0002		59	151	0.0448
	19	171	0.0006		60	130	0.0844		19	191	0.0003		60	150	0.0487
	20	170	0.0007		61	129	0.0909		20	190	0.0004		61	149	0.0527
	21	169	0.0008		62	128	0.0978		21	189	0.0004		62	148	0.0570
	22	168	0.0010		63	127	0.1051		22	188	0.0005		63	147	0.0615
	23	167	0.0012		64	126	0.1127		23	187	0.0006		64	146	0.0664
	24	166	0.0014		65	125	0.1206		24	186	0.0007		65	145	0.0715
	25	165	0.0017		66	124	0.1290		25	185	0.0008		66	144	0.0768
	26	164	0.0020		67	123	0.1377		26	184	0.0010		67	143	0.0825
	27	163	0.0023		68	122	0.1467		27	183	0.0012		68	142	0.0884
	28	162	0.0027		69	121	0.1562		28	182	0.0014		69	141	0.0947
	29	161	0.0031		70	120	0.1660		29	181	0.0016		70	140	0.1012
	30	160	0.0036						30	180	0.0018		71	139	0.1081
	31	159	0.0041						31	179	0.0021		72	138	0.1153
	32	158	0.0047						32	178	0.0024		73	137	0.1227
	33	157	0.0054						33	177	0.0028		74	136	0.1305
	34	156	0.0062						34	176	0.0032		75	135	0.1387
	35	155	0.0070						35	175	0.0036		76	134	0.1471
	36	154	0.0080						36	174	0.0042		77	133	0.1559
	37	153	0.0090						37	173	0.0047				
	38	152	0.0102						38	172	0.0053				
	39	151	0.0115						39	171	0.0060				
	40	150	0.0129						40	170	0.0068				

Table 10 Critical Values for the Wilcoxon Rank-Sum Statistic

This table contains critical values and probabilities for the Wilcoxon rank-sum statistic W = the sum of the ranks of the m observations in the smaller sample: m and n are the sample sizes, and c_1 and c_2 are defined by $P(W \leq c_1) = \alpha$ and $P(W \geq c_2) = \alpha$, respectively.

m	n	c_1	c_2	α
2	3	3	9	0.1000
2	4	3	11	0.0667
		4	10	0.1333
2	5	3	13	0.0476
		4	12	0.0952
2	6	3	15	0.0357
		4	14	0.0714
		5	13	0.1429
2	7	3	17	0.0278
		4	16	0.0556
		5	15	0.1111
2	8	3	19	0.0222
		4	18	0.0444
		5	17	0.0889
		6	16	0.1333
2	9	3	21	0.0182
		4	20	0.0364
		5	19	0.0727
		6	18	0.1091
2	10	3	23	0.0152
		4	22	0.0303
		5	21	0.0606
		6	20	0.0909
		7	19	0.1364
3	3	6	15	0.0500
		7	14	0.1000
3	4	6	18	0.0286
		7	17	0.0571
		8	16	0.1143
3	5	6	21	0.0179
		7	20	0.0357
		8	19	0.0714
		9	18	0.1250
3	6	6	24	0.0119
		7	23	0.0238
		8	22	0.0476
		9	21	0.0833
		10	20	0.1310
3	7	6	27	0.0083
		7	26	0.0167
		8	25	0.0333
		9	24	0.0583
		10	23	0.0917
		11	22	0.1333

m	n	c_1	c_2	α
3	8	6	30	0.0061
		7	29	0.0121
		8	28	0.0242
		9	27	0.0424
		10	26	0.0667
		11	25	0.0970
		12	24	0.1394
3	9	6	33	0.0045
		7	32	0.0091
		8	31	0.0182
		9	30	0.0318
		10	29	0.0500
		11	28	0.0727
		12	27	0.1045
		13	26	0.1409
3	10	6	36	0.0035
		7	35	0.0070
		8	34	0.0140
		9	33	0.0245
		10	32	0.0385
		11	31	0.0559
		12	30	0.0804
13	29	0.1084		
14	28	0.1434		
4	4	10	26	0.0143
		11	25	0.0286
		12	24	0.0571
		13	23	0.1000
4	5	10	30	0.0079
		11	29	0.0159
		12	28	0.0317
		13	27	0.0556
		14	26	0.0952
		15	25	0.1429
4	6	10	34	0.0048
		11	33	0.0095
		12	32	0.0190
		13	31	0.0333
		14	30	0.0571
		15	29	0.0857
		16	28	0.1286

m	n	c_1	c_2	α
4	7	10	38	0.0030
		11	37	0.0061
		12	36	0.0121
		13	35	0.0212
		14	34	0.0364
		15	33	0.0545
		16	32	0.0818
		17	31	0.1152
		18	30	0.1576
4	8	10	42	0.0020
		11	41	0.0040
		12	40	0.0081
		13	39	0.0141
		14	38	0.0242
		15	37	0.0364
		16	36	0.0545
		17	35	0.0768
18	34	0.1071		
19	33	0.1414		
4	9	10	46	0.0014
		11	45	0.0028
		12	44	0.0056
		13	43	0.0098
		14	42	0.0168
		15	41	0.0252
		16	40	0.0378
		17	39	0.0531
		18	38	0.0741
		19	37	0.0993
20	36	0.1301		
4	10	10	50	0.0010
		11	49	0.0020
		12	48	0.0040
		13	47	0.0070
		14	46	0.0120
		15	45	0.0180
		16	44	0.0270
		17	43	0.0380
		18	42	0.0529
		19	41	0.0709
		20	40	0.0939
		21	39	0.1199
22	38	0.1518		

m	n	c_1	c_2	α
5	5	15	40	0.0040
		16	39	0.0079
		17	38	0.0159
		18	37	0.0278
		19	36	0.0476
		20	35	0.0754
		21	34	0.1111
22	33	0.1548		
5	6	15	45	0.0022
		16	44	0.0043
		17	43	0.0087
		18	42	0.0152
		19	41	0.0260
		20	40	0.0411
21	39	0.0628		
22	38	0.0887		
23	37	0.1234		
5	7	15	50	0.0013
		16	49	0.0025
		17	48	0.0051
		18	47	0.0088
		19	46	0.0152
		20	45	0.0240
		21	44	0.0366
22	43	0.0530		
23	42	0.0745		
24	41	0.1010		
25	40	0.1338		
5	8	15	55	0.0008
		16	54	0.0016
		17	53	0.0031
		18	52	0.0054
		19	51	0.0093
		20	50	0.0148
		21	49	0.0225
		22	48	0.0326
		23	47	0.0466
		24	46	0.0637
25	45	0.0855		
26	44	0.1111		
27	43	0.1422		

Table 10 Critical Values for the Wilcoxon Rank-Sum Statistic (Continued)

<i>m</i>	<i>n</i>	<i>c</i> ₁	<i>c</i> ₂	α	<i>m</i>	<i>n</i>	<i>c</i> ₁	<i>c</i> ₂	α	<i>m</i>	<i>n</i>	<i>c</i> ₁	<i>c</i> ₂	α	<i>m</i>	<i>n</i>	<i>c</i> ₁	<i>c</i> ₂	α
7	10	28	98	0.0001	8	9	36	108	0.0000	9	9	45	126	0.0000			73	107	0.0912
		29	97	0.0001			37	107	0.0001			46	125	0.0000			74	106	0.1055
		30	96	0.0002			38	106	0.0002			47	124	0.0001			75	105	0.1214
		31	95	0.0004			39	105	0.0003			48	123	0.0001			76	104	0.1388
		32	94	0.0006			40	104	0.0005			49	122	0.0002					
		33	93	0.0010			41	103	0.0008			50	121	0.0004					
		34	92	0.0015			42	102	0.0012			51	120	0.0006					
		35	91	0.0023			43	101	0.0019			52	119	0.0009					
		36	90	0.0034			44	100	0.0028			53	118	0.0014					
		37	89	0.0048			45	99	0.0039			54	117	0.0020					
		38	88	0.0068			46	98	0.0056			55	116	0.0028					
		39	87	0.0093			47	97	0.0076			56	115	0.0039					
		40	86	0.0125			48	96	0.0103			57	114	0.0053					
		41	85	0.0165			49	95	0.0137			58	113	0.0071					
		42	84	0.0215			50	94	0.0180			59	112	0.0094					
		43	83	0.0277			51	93	0.0232			60	111	0.0122					
		44	82	0.0351			52	92	0.0296			61	110	0.0157					
		45	81	0.0439			53	91	0.0372			62	109	0.0200					
		46	80	0.0544			54	90	0.0464			63	108	0.0252					
		47	79	0.0665			55	89	0.0570			64	107	0.0313					
48	78	0.0806	56	88	0.0694	65	106	0.0385											
49	77	0.0966	57	87	0.0836	66	105	0.0470											
50	76	0.1148	58	86	0.0998	67	104	0.0567											
51	75	0.1349	59	85	0.1179	68	103	0.0680											
52	74	0.1574	60	84	0.1383	69	102	0.0807											
8	8	36	100	0.0001	8	10	36	116	0.0000	9	10	45	135	0.0000	10	10	55	155	0.0000
		37	99	0.0002			37	115	0.0000			46	134	0.0000			56	154	0.0000
		38	98	0.0003			38	114	0.0001			47	133	0.0000			57	153	0.0000
		39	97	0.0005			39	113	0.0002			48	132	0.0001			58	152	0.0000
		40	96	0.0009			40	112	0.0003			49	131	0.0001			59	151	0.0001
		41	95	0.0015			41	111	0.0004			50	130	0.0002			60	150	0.0001
		42	94	0.0023			42	110	0.0007			51	129	0.0003			61	149	0.0002
		43	93	0.0035			43	109	0.0010			52	128	0.0005			62	148	0.0002
		44	92	0.0052			44	108	0.0015			53	127	0.0007			63	147	0.0004
		45	91	0.0074			45	107	0.0022			54	126	0.0011			64	146	0.0005
		46	90	0.0103			46	106	0.0031			55	125	0.0015			65	145	0.0008
		47	89	0.0141			47	105	0.0043			56	124	0.0021			66	144	0.0010
		48	88	0.0190			48	104	0.0058			57	123	0.0028			67	143	0.0014
		49	87	0.0249			49	103	0.0078			58	122	0.0038			68	142	0.0019
		50	86	0.0325			50	102	0.0103			59	121	0.0051			69	141	0.0026
		51	85	0.0415			51	101	0.0133			60	120	0.0066			70	140	0.0034
		52	84	0.0524			52	100	0.0171			61	119	0.0086			71	139	0.0045
		53	83	0.0652			53	99	0.0217			62	118	0.0110			72	138	0.0057
		54	82	0.0803			54	98	0.0273			63	117	0.0140			73	137	0.0073
		55	81	0.0974			55	97	0.0338			64	116	0.0175			74	136	0.0093
56	80	0.1172	56	96	0.0416	65	115	0.0217	75	135	0.0116								
57	79	0.1393	57	95	0.0506	66	114	0.0267	76	134	0.0144								
			58	94	0.0610	67	113	0.0326	77	133	0.0177								
			59	93	0.0729	68	112	0.0394	78	132	0.0216								
			60	92	0.0864	69	111	0.0474	79	131	0.0262								
			61	91	0.1015	70	110	0.0564	80	130	0.0315								
			62	90	0.1185	71	109	0.0667	81	129	0.0376								
			63	89	0.1371	72	108	0.0782	82	128	0.0446								
			64	88	0.1577				83	127	0.0526								
									84	126	0.0615								
									85	125	0.0716								
									86	124	0.0827								
									87	123	0.0952								
									88	122	0.1088								
									89	121	0.1237								
									90	120	0.1399								
									91	119	0.1575								

Table 11 Critical Values for the Runs Test

This table contains cumulative probabilities associated with the runs test. Let m be the number of observations in one category, n be the number of observations in the other category ($m \leq n$), and V be the number of runs. The values in this table are the probabilities $P(V \leq v)$ if the order of observations is random.

m	n	2	3	4	5	6	7	8	9
2	2	0.3333	0.6667	1.0000					
2	3	0.2000	0.5000	0.9000	1.0000				
2	4	0.1333	0.4000	0.8000	1.0000				
2	5	0.0952	0.3333	0.7143	1.0000				
2	6	0.0714	0.2857	0.6429	1.0000				
2	7	0.0556	0.2500	0.5833	1.0000				
2	8	0.0444	0.2222	0.5333	1.0000				
2	9	0.0364	0.2000	0.4909	1.0000				
2	10	0.0303	0.1818	0.4545	1.0000				
3	3	0.1000	0.3000	0.7000	0.9000	1.0000			
3	4	0.0571	0.2000	0.5429	0.8000	0.9714	1.0000		
3	5	0.0357	0.1429	0.4286	0.7143	0.9286	1.0000		
3	6	0.0238	0.1071	0.3452	0.6429	0.8810	1.0000		
3	7	0.0167	0.0833	0.2833	0.5833	0.8333	1.0000		
3	8	0.0121	0.0667	0.2364	0.5333	0.7879	1.0000		
3	9	0.0091	0.0545	0.2000	0.4909	0.7455	1.0000		
3	10	0.0070	0.0455	0.1713	0.4545	0.7063	1.0000		
4	4	0.0286	0.1143	0.3714	0.6286	0.8857	0.9714	1.0000	
4	5	0.0159	0.0714	0.2619	0.5000	0.7857	0.9286	0.9921	1.0000
4	6	0.0095	0.0476	0.1905	0.4048	0.6905	0.8810	0.9762	1.0000
4	7	0.0061	0.0333	0.1424	0.3333	0.6061	0.8333	0.9545	1.0000
4	8	0.0040	0.0242	0.1091	0.2788	0.5333	0.7879	0.9293	1.0000
4	9	0.0028	0.0182	0.0853	0.2364	0.4713	0.7455	0.9021	1.0000
4	10	0.0020	0.0140	0.0679	0.2028	0.4186	0.7063	0.8741	1.0000

Table 11 Critical Values for the Runs Test (Continued)

<i>m</i>	<i>n</i>	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
5	5	0.0079	0.0397	0.1667	0.3571	0.6429	0.8333	0.9603	0.9921	1.0000										
5	6	0.0043	0.0238	0.1104	0.2619	0.5216	0.7381	0.9113	0.9762	0.9978	1.0000									
5	7	0.0025	0.0152	0.0758	0.1970	0.4242	0.6515	0.8535	0.9545	0.9924	1.0000									
5	8	0.0016	0.0101	0.0536	0.1515	0.3473	0.5758	0.7933	0.9293	0.9837	1.0000									
5	9	0.0010	0.0070	0.0390	0.1189	0.2867	0.5105	0.7343	0.9021	0.9720	1.0000									
5	10	0.0007	0.0050	0.0290	0.0949	0.2388	0.4545	0.6783	0.8741	0.9580	1.0000									
6	6	0.0022	0.0130	0.0671	0.1753	0.3918	0.6082	0.8247	0.9329	0.9870	0.9978	1.0000								
6	7	0.0012	0.0076	0.0425	0.1212	0.2960	0.5000	0.7331	0.8788	0.9662	0.9924	0.9994	1.0000							
6	8	0.0007	0.0047	0.0280	0.0862	0.2261	0.4126	0.6457	0.8205	0.9371	0.9837	0.9977	1.0000							
6	9	0.0004	0.0030	0.0190	0.0629	0.1748	0.3427	0.5664	0.7622	0.9021	0.9720	0.9944	1.0000							
6	10	0.0002	0.0020	0.0132	0.0470	0.1369	0.2867	0.4965	0.7063	0.8636	0.9580	0.9895	1.0000							
7	7	0.0006	0.0041	0.0251	0.0775	0.2086	0.3834	0.6166	0.7914	0.9225	0.9749	0.9959	0.9994	1.0000						
7	8	0.0003	0.0023	0.0154	0.0513	0.1492	0.2960	0.5136	0.7040	0.8671	0.9487	0.9879	0.9977	0.9998	1.0000					
7	9	0.0002	0.0014	0.0098	0.0350	0.1084	0.2308	0.4266	0.6224	0.8059	0.9161	0.9748	0.9944	0.9993	1.0000					
7	10	0.0001	0.0009	0.0064	0.0245	0.0800	0.1818	0.3546	0.5490	0.7433	0.8794	0.9571	0.9895	0.9981	1.0000					
8	8	0.0002	0.0012	0.0089	0.0317	0.1002	0.2145	0.4048	0.5952	0.7855	0.8998	0.9683	0.9911	0.9988	0.9998	1.0000				
8	9	0.0001	0.0007	0.0053	0.0203	0.0687	0.1573	0.3186	0.5000	0.7016	0.8427	0.9394	0.9797	0.9958	0.9993	1.0000	1.0000			
8	10	0.0000	0.0004	0.0033	0.0134	0.0479	0.1170	0.2514	0.4194	0.6209	0.7822	0.9031	0.9636	0.9905	0.9981	0.9998	1.0000	1.0000		
9	9	0.0000	0.0004	0.0030	0.0122	0.0445	0.1090	0.2380	0.3992	0.6008	0.7620	0.8910	0.9555	0.9878	0.9970	0.9996	1.0000	1.0000		
9	10	0.0000	0.0002	0.0018	0.0076	0.0294	0.0767	0.1786	0.3186	0.5095	0.6814	0.8342	0.9233	0.9742	0.9924	0.9986	0.9998	1.0000	1.0000	1.0000
10	10	0.0000	0.0001	0.0010	0.0045	0.0185	0.0513	0.1276	0.2422	0.4141	0.5859	0.7578	0.8724	0.9487	0.9815	0.9955	0.9990	0.9999	1.0000	1.0000

Table 12 Greek Alphabet

This table contains the Greek alphabet: the letter name, the lowercase letter, the variant of the lowercase letter where applicable, and the uppercase letter.

Name	Lowercase letter	Lowercase variant	Uppercase letter
Alpha	α		A
Beta	β		B
Gamma	γ		Γ
Delta	δ		Δ
Epsilon	ε	ϵ	E
Zeta	ζ		Z
Eta	η		H
Theta	θ	ϑ	Θ
Iota	ι		I
Kappa	κ		K
Lambda	λ		Λ
Mu	μ		M
Nu	ν		N
Xi	ξ		Ξ
Omicron	o		O
Pi	π	ρ	Π
Rho	ρ	ϱ	R
Sigma	σ	ς	Σ
Tau	τ		T
Upsilon	υ		Υ
Phi	ϕ	φ	Φ
Chi	χ		X
Psi	ψ		Ψ
Omega	ω		Ω

